

to show $CD < BD$

proof

In $\triangle ABC$, $AB = AC$

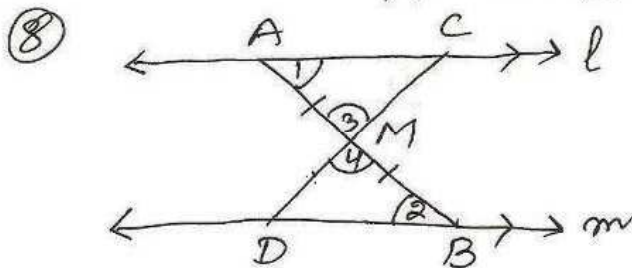
$$\angle C = \angle ABC$$

(uses \triangle prop.)

But $\angle ABC > \angle 1$

$$\angle C > \angle 1$$

$BD > CD$ [greater angle has longer side opp. to it]



to show $MC = MD$

proof $l \parallel m$

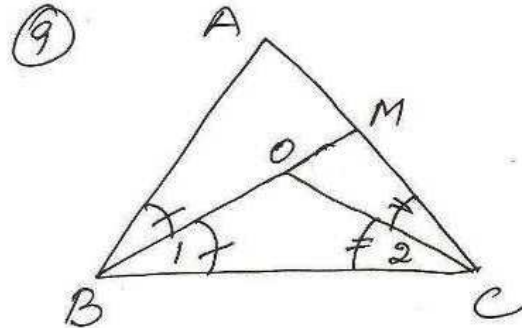
$\therefore \angle 1 = \angle 2$ (alter. interior angles)

$AM = BM$ (given)

$\angle 3 = \angle 4$ (vert opp \angle s)

$\therefore \triangle AMC \cong \triangle BMD$ by ASA prop

$$MC = MD \text{ (C.P.C.T.)}$$



to prove $\angle MOC = \angle ABC$

proof In $\triangle ABC$

$$AB = AC$$

$$\angle ACB = \angle ABC \text{ (uses } \triangle \text{ prop.)}$$

$$\angle L_2 = \angle L_1 \text{ [BO bis. } \angle ABC \text{ CO bis. } \angle ACB \text{]} \dots \textcircled{1}$$

$$\begin{aligned} \angle MOC &= \angle 1 + \angle L_2 \text{ (exterior } \angle \text{ prop of } \triangle) \\ &= \angle 1 + \angle 1 \\ &= 2\angle 1 \end{aligned}$$

$$= \angle ABC$$