

$$2 \text{ (v)} \quad ax^2 + bx + c = 0$$

$\therefore a, c$ have opposite signs

$\therefore ac$ is -ve

$$D = b^2 - 4ac \\ = b^2 - 4(\text{-ve value})$$

$$\therefore D > 0$$

True

$$2 \text{ (vi)} \quad ax^2 + bx + c = 0$$

a, c have same sign

$\therefore ac$ is +ve.

$$D = b^2 - 4ac \\ = 0^2 - 4(\text{+ve value})$$

$$D < 0$$

\therefore no real roots

③ False

$x^2 - 3 = 0$ has integral coeff. but roots are $\pm\sqrt{3}$ which are not integral

④ yes

$x^2 - 3 = 0$ has integral coeff. but both roots are irrational ($\pm\sqrt{3}$)

⑤ yes

$\sqrt{7}x^2 + 2\sqrt{7}x - 3\sqrt{7} = 0$
has rational roots
1, -3

$$\text{⑥ LHS} = (0.2)^2 - 0.4 \\ = 0.04 - 0.4 \\ = -0.36 \\ \neq 0$$

$\therefore 0.2$ is not a root of $x^2 - 0.4 = 0$

⑦ yes $x^2 + bx + c = 0$

$$\text{if } b = 0 \\ x^2 + c = 0$$

$$\Rightarrow x^2 = -c$$

$$\Rightarrow x = \pm\sqrt{-c} \quad \left[\begin{array}{l} \text{+ve as} \\ \text{-c is} \\ \text{+ve as} \\ \text{c is -ve} \end{array} \right]$$