

$$\textcircled{\text{vii}} \quad \sqrt{2}x^2 - \frac{3}{\sqrt{2}}x + \frac{1}{\sqrt{2}} = 0$$

$$D = b^2 - 4ac$$

$$= \left(-\frac{3}{\sqrt{2}}\right)^2 - 4 \times \sqrt{2} \times \frac{1}{\sqrt{2}}$$

$$= \frac{9}{2} - 4$$

$$= \frac{9-8}{2}$$

$$= \frac{1}{2}$$

$$\therefore D > 0$$

\therefore two distinct real roots

$$\textcircled{\text{viii}} \quad x(1-x) - 2 = 0$$

$$\Rightarrow x - x^2 - 2 = 0$$

$$\Rightarrow x^2 - x + 2 = 0$$

$$D = b^2 - 4ac$$

$$= (-1)^2 - 4 \times 1 \times 2$$

$$= 1 - 8$$

$$= -7$$

$$\therefore D < 0$$

no real roots

$$\textcircled{\text{ix}} \quad (x-1)(x+2) + 2 = 0$$

$$\Rightarrow x^2 + x - \cancel{2} + \cancel{2} = 0$$

$$\Rightarrow x^2 + x = 0$$

$$D = b^2 - 4ac$$

$$= 1^2 - 4 \times 1 \times 0$$

$$= 1 - 0$$

$$= 1$$

$$\therefore D > 0$$

two distinct real roots

$$\textcircled{\text{x}} \quad (x+1)(x-2) + x = 0$$

$$\Rightarrow x^2 - \cancel{x} - 2 + \cancel{x} = 0$$

$$\Rightarrow x^2 - 2 = 0$$

$$D = b^2 - 4ac$$

$$= 0^2 - 4 \times 1 \times -2$$

$$= 0 + 8$$

$$= 8$$

$$\therefore D > 0$$

two distinct real roots.

2① False

[It has at the most 2 real roots]

② False

$x^2 + 4 = 0$ has no real roots.

③ False $x^2 + 4 = 0$ has no real roots.

④ True

\therefore true