

$$\begin{aligned}
 \textcircled{1} \quad \text{LHS} &= \frac{\tan 47^\circ}{\cot 43^\circ} \\
 &= \frac{\cot(90^\circ - 47^\circ)}{\cot 43^\circ} \\
 &= \frac{\cot 43^\circ}{\cot 43^\circ} \\
 &= 1 \\
 &= \text{RHS True}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{2} \quad \cos^2 23^\circ - \sin^2 67^\circ \\
 &= \sin^2(90^\circ - 23^\circ) - \sin^2 67^\circ \\
 &= \sin^2 67^\circ - \sin^2 67^\circ \\
 &= 0 \quad \text{False}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{3} \quad \sin 80^\circ - \cos 80^\circ \\
 &= \sin 80^\circ - \sin(90^\circ - 80^\circ) \\
 &= \sin 80^\circ - \sin 10^\circ \\
 &\text{is +ve} \\
 &\because \sin \theta \text{ increases as } \\
 &\quad \theta \text{ increases False}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{4} \quad \text{LHS} &= \sqrt{(1 - \cos^2 \theta) \sec^2 \theta} \\
 &= \sqrt{\sin^2 \theta \times \frac{1}{\cos^2 \theta}} \\
 &= \sqrt{\tan^2 \theta} \\
 &= \tan \theta \quad \text{True}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{5} \quad \cos A + \cos^2 A &= 1 \\
 \Rightarrow \cos A &= 1 - \cos^2 A \\
 \Rightarrow \cos A &= \sin^2 A \dots \textcircled{1} \\
 \text{LHS} &= \sin^2 A + \sin^4 A \\
 &= \sin^2 A (1 + \sin^2 A) \\
 &= \cos A (1 + \cos A) \\
 &\quad \text{using (i)} \\
 &= \cos A + \cos^2 A \\
 &= 1 \quad (\text{given}) \\
 &= \text{RHS True}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{6} \quad \text{LHS} &= (\tan \theta + 2)(2 \tan \theta + 1) \\
 &= 2 \tan^2 \theta + \tan \theta + 4 \tan \theta + 2 \\
 &= 2 \tan^2 \theta + 5 \tan \theta + 2 \\
 &= 1 + \tan^2 \theta + 1 + \tan^2 \theta + 5 \tan \theta \\
 &= \sec^2 \theta + \sec^2 \theta + 5 \tan \theta \\
 &\quad [\because 1 + \tan^2 \theta = \sec^2 \theta] \\
 &= 2 \sec^2 \theta + 5 \tan \theta \\
 &\neq \text{RHS} \quad \text{False}
 \end{aligned}$$