

$$(16) \bar{x} = \frac{x_1 + x_2 + x_3 + \dots + x_n}{n}$$

$$\Rightarrow n\bar{x} = x_1 + x_2 + x_3 + \dots + x_n \quad \text{--- (1)}$$

reqd. Mean

$$= \frac{ax_1 + ax_2 + ax_3 + \dots + ax_n + \frac{x_1}{a} + \frac{x_2}{a} + \frac{x_3}{a} + \dots + \frac{x_n}{a}}{2n}$$

$$= \frac{a(x_1 + x_2 + x_3 + \dots + x_n) + \frac{1}{a}(x_1 + x_2 + x_3 + \dots + x_n)}{2n}$$

$$= \frac{an\bar{x} + \frac{n\bar{x}}{a}}{2n}$$

$$\bar{x} \left(a + \frac{1}{a} \right) \quad \text{(B)}$$

(17)

$$\bar{x}_1 = x_1 + x_2 + x_3 + \dots + x_{n_1}$$

$$\Rightarrow n_1 \bar{x}_1 = x_1 + x_2 + x_3 + \dots + x_{n_1} \quad \text{--- (i)}$$

Similarly

$$n_2 \bar{x}_2 = x_1 + x_2 + x_3 + \dots + x_{n_2} \quad \text{--- (ii)}$$

$$n_3 \bar{x}_3 = x_1 + x_2 + x_3 + \dots + x_{n_3} \quad \text{--- (iii)}$$

⋮

$$n_m \bar{x}_m = x_1 + x_2 + x_3 + \dots + x_{n_m} \quad \text{--- (m)}$$

$$\bar{x} = \frac{n_1 \bar{x}_1 + n_2 \bar{x}_2 + n_3 \bar{x}_3 + \dots + n_m \bar{x}_m}{n_1 + n_2 + n_3 + \dots + n_m}$$

$$= \frac{\sum_{i=1}^m n_i \bar{x}_i}{\sum_{i=1}^m n_i} \quad \text{(C)}$$