

12. Mean = 9

$$\frac{x+x+3+x+5+x+7+x+10}{5} = 9$$

$$\Rightarrow 5x + 25 = 45$$

$$\Rightarrow 5x = 20$$

$$\Rightarrow x = 4$$

last 3 obs. are

$$4+5, 4+7, 4+10$$

$$= 9, 11, 14$$

$$\text{Mean} = \frac{9+11+14}{3}$$

$$= \frac{34}{3}$$

$$= 11\frac{1}{3} \text{ (C)}$$

12. $\bar{x} = \frac{x_1+x_2+x_3+\dots+x_n}{n}$

$$\Rightarrow n\bar{x} = x_1+x_2+x_3+\dots+x_n \quad \text{--- (1)}$$

$$\sum_{i=1}^n (x_i - \bar{x})$$

$$= x_1 - \bar{x} + x_2 - \bar{x} + x_3 - \bar{x} + \dots + x_n - \bar{x}$$

$$= x_1 + x_2 + x_3 + \dots + x_n - n\bar{x}$$

$$= n\bar{x} - n\bar{x} \quad \text{[use (1)]}$$

$$= 0 \quad \text{(B)}$$

ex 14.1, exemplar ix

(14) let obs. be

$$x_1, x_2, x_3, \dots, x_n$$

$$\bar{x}(\text{Mean}) = \frac{x_1+x_2+x_3+\dots+x_n}{n}$$

$$\Rightarrow n\bar{x} = x_1+x_2+x_3+\dots+x_n \quad \text{--- (1)}$$

Increased obs

$$x_1+5, x_2+5, x_3+5, \dots, x_n+5$$

New Mean

$$= \frac{x_1+5+x_2+5+x_3+5+\dots+x_n+5}{n}$$

$$= \frac{x_1+x_2+x_3+\dots+x_n + 5n}{n}$$

$$= \frac{n\bar{x} + 5n}{n} \quad \text{(use (1))}$$

$$= \frac{n(\bar{x} + 5)}{n}$$

$$= \bar{x} + 5$$

is increased by 5

(D)

(15)

$$\bar{x} = \frac{x_1+x_2+x_3+\dots+x_n}{n}$$

$$\Rightarrow n\bar{x} = x_1+x_2+x_3+\dots+x_n \quad \text{--- (1)}$$

Sum

$$n\bar{y} = y_1+y_2+y_3+\dots+y_n \quad \text{--- (1)}$$

$$\bar{z} = \frac{x_1+x_2+x_3+\dots+x_n + y_1+y_2+y_3+\dots+y_n}{2n}$$

$$= \frac{n\bar{x} + n\bar{y}}{2n} = \frac{\bar{x} + \bar{y}}{2} \quad \text{(B)}$$