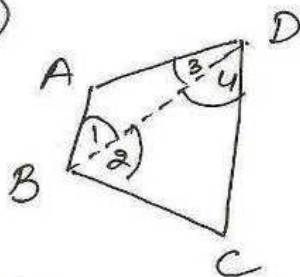


(19)



given AB is shortest, CD - largest side of $\square ABCD$

to check $\angle B > \angle D$ or $\angle D > \angle B$

const - join BD

proof In $\triangle ABD$

$$AD > AB$$

$\Rightarrow \angle 1 > \angle 3$ [longer side has greater angle opp. to it] ... (i)

In $\triangle BCD$

$$CD > BC$$

$$\Rightarrow \angle 2 > \angle 4 \quad (\text{do})$$

... (ii)

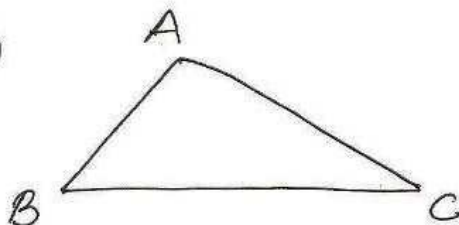
$$\text{(i)} + \text{(ii)}$$

$$\angle 1 + \angle 2 > \angle 3 + \angle 4$$

$$\angle B > \angle D$$

ex 7.4

(20)



to prove $\angle A > \frac{2}{3}$ rt \angle

proof In $\triangle ABC$

$$BC > AB$$

$$\angle A > \angle C \quad \dots \text{(i)}$$

[In a \triangle longer side has greater angle opp. to it]

$$BC > AC$$

$$\Rightarrow \angle A > \angle B \quad \dots \text{(ii)}$$

$$\text{(i)} + \text{(ii)}$$

$$2\angle A > \angle B + \angle C$$

adding $\angle A$ on both sides

$$3\angle A > \angle A + \angle B + \angle C$$

$$3\angle A > 180^\circ$$

$$\Rightarrow \angle A > \frac{180}{3}$$

$$> \frac{2}{3} \times 90$$

$$\Rightarrow \angle A > \frac{2}{3} \text{ rt angle}$$