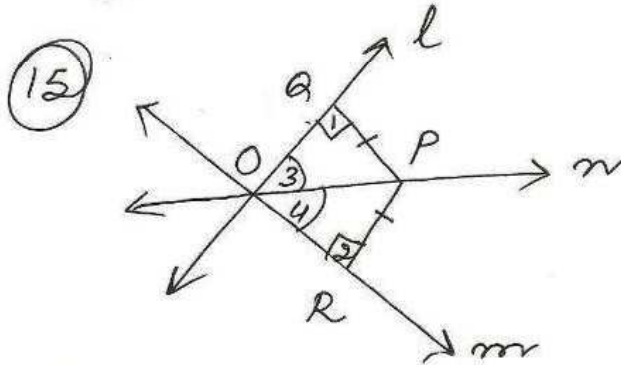


to prove  $BE = \frac{1}{2} AC$   
 const - produce  $BE$  to  $D$   
 s.t.  $ED = BE$  join  
 $AD, CD$

proof  $ED = EB$   
 $EA = EC$

$\therefore \square ABCD$  is a  $\square$   
 $\angle ABC = 90^\circ$   
 $\therefore$   $\square ABCD$  is a rect.

$AC = BD$  [diagonals of rect.]  
 $\frac{1}{2} AC = \frac{1}{2} BD$   
 $\frac{1}{2} AC = BE$  [ $BE = ED$ ]



To prove -  $m$  is bisector of  $\angle AOR$

proof In  $\triangle OAP$  and  $\triangle ORP$

$\angle 1 = \angle 2 = 90^\circ$

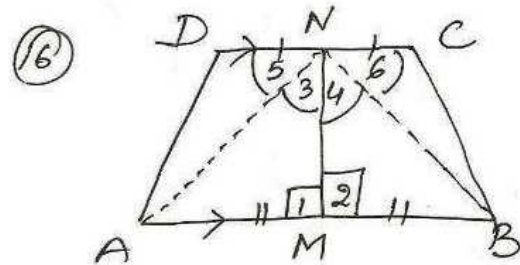
$OP = OP$

$PA = PR$  (given)

$\therefore \triangle OAP \cong \triangle ORP$  by RHS prop

$\Rightarrow \angle 3 = \angle 4$  (Cpct)

$\therefore m$  is bisector of  $\angle AOR$



to prove  $AD = BC$   
 const - join  $AN, BN$   
 proof - In  $\triangle AMN$  and  $\triangle BMN$

$AM = BM$  (given)

$\angle 1 = \angle 2 = 90^\circ$

$NM = NM$

$\therefore \triangle AMN \cong \triangle BMN$  by SAS prop

$\angle 3 = \angle 4$  (Cpct)

$AN = BN$  (do)

$\angle DNM = \angle CNM = 90^\circ$

$\angle 5 + \angle 6 = \angle 4 + \angle 3$  [ $\because \angle 3 = \angle 4$ ]

In  $\triangle ADN$  and  $\triangle BCN$   
 $DN = CN$  |  $\therefore \triangle ADN \cong \triangle BCN$   
 $\angle 5 = \angle 6$  | by SAS prop  
 $AN = BN$  |  $AD = BC$  (Cpct)