

to show $\square BFDE$ is a $\parallel gm$

proof $ABCD$ is a $\parallel gm$

$\therefore OD = OB \dots (i)$ [diags of $\parallel gm$ bisect each other]
 $OA = OC \dots (ii)$

$AE = CF \dots (iii)$ (given)

$(i) - (iii)$

$$OA - AE = OC - CF$$

$$\Rightarrow OE = OF \dots (iv)$$

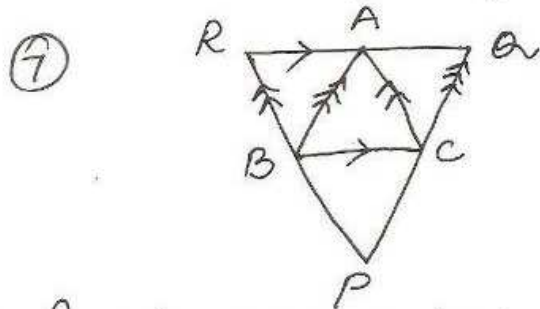
$\square BFDE$ is a $\parallel gm$ ($OB = OD$, $OE = OF$)

proof - In $\triangle ADC$, E is midpt. of AD and $EF \parallel DC$

$$\left[\begin{array}{l} EF \parallel AB \\ DC \parallel AB \\ \Rightarrow AB \parallel EF \parallel DC \end{array} \right]$$

$\therefore O$ is midpt. of AC
 [converse of midpt. theorem]

In $\triangle CAB$, O is midpt AC, $OF \parallel AB$
 $\Rightarrow OF$ bisects CB (do)
 $\therefore F$ is midpt of BC



Proof $\square RBCA$ is a $\parallel gm$
 $[RA \parallel BC]$
 $[BR \parallel CA]$

$\therefore RA = BC \dots (i)$ (opp. sides of a $\parallel gm$)

$\square RBCA$ is a $\parallel gm$

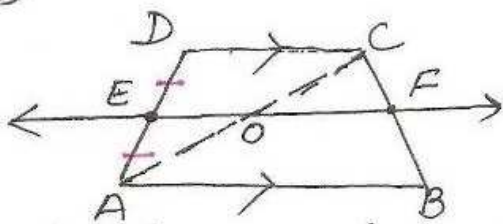
$$AR = BC \dots (ii) \text{ (do)}$$

$$(i) + (ii)$$

$$RA + AR = 2BC$$

$$\Rightarrow BC = \frac{1}{2} AR$$

6



const - form AC intersecting AC at O