

⑤ given - In fig.  $OP = OQ = 3\text{cm}$   
 $O'P = O'Q = 4\text{cm}$   
 $OP$  and  $O'P$  are tangents

to find  $PA$

proof  $OP = OQ = 3\text{cm}$

$O'P = O'Q = 4\text{cm}$

$\therefore \square OPO'Q$  is a kite

$\Rightarrow PQ \perp OO'$  [diagonals of a kite are  $\perp$  to each other]

$\therefore \angle' = 90^\circ$

$\angle O'PO = 90^\circ$  [radius  $\perp$  tangent]

In rt  $\triangle O'PO$

$(OO')^2 = (O'P)^2 + (OP)^2$  [Pythagoras theorem]

$$= 4^2 + 3^2$$

$$= 16 + 9$$

$$= 25$$

$$\Rightarrow OO' = \sqrt{25}$$

$$= 5\text{cm}$$

$$s = \frac{a+b+c}{2}$$

$$= \frac{3+4+5}{2}$$

$$= \frac{12}{2}$$

$$= 6\text{cm}$$

$$\text{ar}(\triangle O'PO) = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{6(6-3)(6-4)(6-5)}$$

$$= \sqrt{6 \times 3 \times 2 \times 1}$$

$$= 6\text{cm}^2$$

