

$$\text{(iv)} \quad \text{ar}(\triangle BDE) = \text{ar}(\triangle ADE) \quad \left[ \begin{array}{l} \Delta s \text{ on same} \\ \text{base and} \\ \text{between} \\ \text{same } \parallel \text{ lines} \end{array} \right]$$

$$\text{ar}(\triangle BDE) - \text{ar}(\triangle DEF) = \text{ar}(\triangle ADE) - \text{ar}(\triangle DEF)$$

$$\Rightarrow \text{ar}(\triangle BFE) = \text{ar}(\triangle AFD)$$

$$\text{(v)} \quad \text{ar}(\triangle BED) = \frac{1}{4} \text{ar}(\triangle ABC) \quad (\text{Proved})$$

$$\frac{1}{2} \times BD \times h_2 = \frac{1}{4} \times \frac{1}{2} \times BC \times AD$$

In an  
[equilateral  $\Delta$   
altitude is also  
median

$$\frac{1}{2} \times h_2 = \frac{1}{4} \times \frac{1}{2} \times h_1, \quad \left[ \begin{array}{l} \therefore AD \perp BC \end{array} \right]$$

$$h_2 = \frac{1}{2} h_1, \dots \textcircled{1}$$

$$\text{ar}(\triangle BFE) = \text{ar}(\triangle AFD)$$

$$\frac{1}{2} \times BF \times h_2 = \frac{1}{2} \times FD \times h_1$$

$$BF \times \frac{1}{2} h_1 = FD \times h_1$$

$$BF = 2FD$$

$$\frac{\text{ar}(\triangle BFE)}{\text{ar}(\triangle FED)} = \frac{\frac{1}{2} \times BF \times \frac{h_1}{2}}{\frac{1}{2} \times FD \times \frac{h_1}{2}}$$

$$= \frac{2FD}{FD} \quad (\because BF = 2FD)$$

$$\text{ar}(\triangle BFE) = 2 \text{ar}(\triangle FED)$$