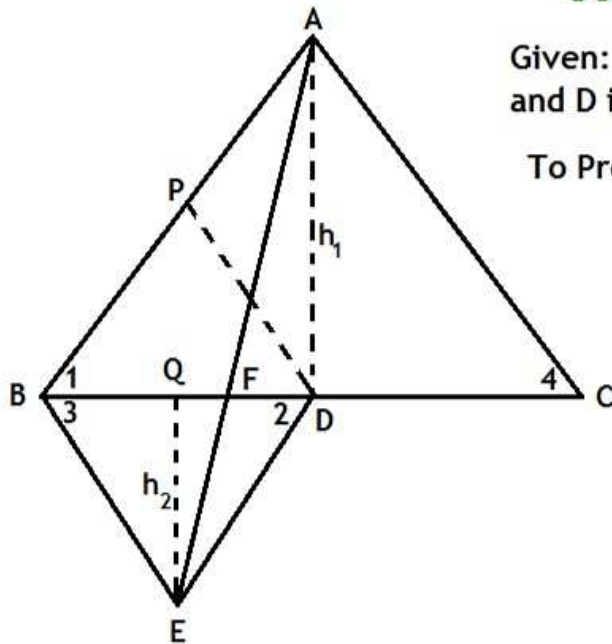


Solution by Dev Anoop (Bathinda)



Given: In figure Triangles ABC and BDE are equilateral and D is the midpoint of BC.

To Prove: $\text{ar}(\text{BDE}) = \frac{1}{4} \text{ar}(\text{ABC})$, $\text{ar}(\text{ABC}) = 2\text{ar}(\text{BEC})$,
 $\text{ar}(\text{BDE}) = \frac{1}{2}\text{ar}(\text{BAE})$, $\text{ar}(\text{BFE}) = \text{ar}(\text{AFD})$,
 $\text{ar}(\text{BFE}) = 2\text{ar}(\text{FED})$, $\text{ar}(\text{FED}) = \frac{1}{8} \text{ar}(\text{AFC})$

let $BE = ED = BD = x$ units

$$BC = 2BD \\ = 2x$$

$$AB = AC = BC = 2x$$

$$\begin{aligned} \textcircled{1} \quad \frac{\text{ar}(\Delta BDE)}{\text{ar}(\Delta ABC)} &= \frac{\frac{\sqrt{3}}{4} s_1^2}{\frac{\sqrt{3}}{4} s_2^2} \\ &= \frac{x^2}{(2x)^2} \\ &= \frac{x^2}{4x^2} \\ &= \frac{1}{4} \end{aligned}$$

$$\Rightarrow \text{ar}(\Delta BDE) = \frac{1}{4} \text{ar}(\Delta ABC)$$

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