

$$\frac{\text{ar}(\triangle YAB)}{\text{ar}(\triangle YZX)} = \frac{\frac{1}{2} \times AB \times YA}{\frac{1}{2} \times ZX \times YP}$$

$$= \frac{AB \times c}{2AB \times 2c} \quad \left[\begin{array}{l} \because ZX = 2AB \\ YA = c \\ YP = 2c \end{array} \right]$$

$$= \frac{1}{4}$$

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$$\Rightarrow \text{ar}(\triangle YAB) = \frac{1}{4} \text{ar}(\triangle YZX)$$

$$= \frac{1}{4} \times \frac{1}{2} \text{ar}(\text{||gm } WXYZ)$$

[\because diagonal divides a ||gm into 2 Δ s equal in area]

$$\Rightarrow \text{ar}(\triangle YAB) = \frac{1}{8} \text{ar}(\text{||gm } WXYZ) \dots \textcircled{i}$$

$$\text{ar}(\triangle WXB) = \frac{1}{2} \times BX \times WR$$

$$= \frac{1}{2} \times \frac{1}{2} \times XY \times WR \quad \left[\begin{array}{l} BX = \frac{1}{2} XY \\ \because B \text{ is midpt. of } XY \end{array} \right]$$

$$\Rightarrow \text{ar}(\triangle WXB) = \frac{1}{4} \text{ar}(\text{||gm } WXYZ) \dots \textcircled{ii}$$

$$\text{Similarly } \text{ar}(\triangle WZA) = \frac{1}{4} \text{ar}(\text{||gm } WXYZ) \dots \textcircled{iii}$$

now

$$\text{ar}(\text{||gm } WXYZ) = \text{ar}(\triangle YAB) + \text{ar}(\triangle YZX) + \text{ar}(\triangle WXB) + \text{ar}(\triangle WZA)$$

$$= \frac{1}{8} \text{ar}(\text{||gm } WXYZ) + \frac{1}{4} \text{ar}(\text{||gm } WXYZ) + \frac{1}{4} \text{ar}(\text{||gm } WXYZ) + \text{ar}(\triangle WAB)$$

$$\Rightarrow \text{ar}(\triangle WAB) = \text{ar}(\text{||gm } WXYZ) - \frac{1}{4} \text{ar}(\text{||gm } WXYZ) - \frac{1}{4} \text{ar}(\text{||gm } WXYZ) - \frac{1}{8} \text{ar}(\text{||gm } WXYZ)$$

$$= \frac{8 \text{ar}(\text{||gm } WXYZ) - 2 \text{ar}(\text{||gm } WXYZ) \times 2 - \text{ar}(\text{||gm } WXYZ)}{8}$$

$$= \frac{3}{8} \text{ar}(\text{||gm } WXYZ)$$