

Find HCF of 384 and 26 and verify HCF is linear combination of 384, 26.

let $a = 384$, $b = 26$

applying euclids div. lemma

$$\begin{array}{r} 26 \overline{) 384} \quad 14 \\ \underline{364} \\ 20 \\ 20 \overline{) 26} \quad 1 \\ \underline{20} \\ 6 \\ 6 \overline{) 20} \quad 3 \\ \underline{18} \\ 2 \\ 2 \overline{) 6} \quad 3 \\ \underline{6} \\ 0 \end{array}$$

$$384 = 26 \times 14 + 20 \dots \textcircled{i}$$

$$\because r \neq 0$$

$$26 = 20 \times 1 + 6 \dots \textcircled{ii}$$

$$\because r \neq 0$$

$$20 = 6 \times 3 + 2 \dots \textcircled{iii}$$

$$\because r \neq 0$$

$$6 = 2 \times 3 + 0$$

$$\because r = 0$$

$\therefore$ HCF of 384 and 26 = 2

using $\textcircled{i}$ $a = 14b + 20 \Rightarrow 20 = a - 14b \dots \textcircled{iv}$

using $\textcircled{ii}$ $6 = 26 - 20 \Rightarrow 6 = b - (a - 14b)$ using $\textcircled{iv}$

$$\Rightarrow 6 = 15b - a \dots \textcircled{v}$$

using $\textcircled{iii}$ $2 = 20 - 6 \times 3$
 $= (a - 14b) - (15b - a)3$ [using $\textcircled{iv}$ and $\textcircled{v}$]

$$\Rightarrow 2 = 4a - 59b$$

$$\Rightarrow 2 = 4 \times a + (-59)b$$

$$\Rightarrow d = na + mb$$

where $d = \text{HCF} = 2$ $n = 4$ $m = -59$